

Quadratic Assignment Procedures (QAP)

Testing hypotheses among networks

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Notes

Change of plans

Decided to change topics for those that show an integration of SNA with other fields

- QAP correlation and Regression
- Affiliation Networks (Real World Data)
- Key Actor Analysis (Regression using centrality measures)
- Text Mining techniques using Social Media Data

Notes

Purpose

Why Hypothesis testing?

- Techniques were designed to test theories about social interactions.
- Provide a sense of how much confidence we can have that the pattern we see in the data we've collected is actually typical of some larger population.
- Yet, inferential statistics in SNA are perhaps **the most sub-utilized set of techniques**

Purpose At the end of the session the participants are expected to understand and replicate the procedures followed to conduct QAP correlation and regression to test hypothesis about networks using UCINET.

Notes

Today we will see the following:

- 1 QAP correlation
 - Motivation
 - UCINET implementation
- 2 QAP Regression
 - Data and preparation
 - UCINET implementation

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QAP correlation

- Correlation between two networks with the same actors (we need one-mode networks).
- **Motivation:** Tests the following statements
 - Professors who are friends also publish together.
 - Professors who publish together also are friends.
 - Countries send diplomats to countries from which they import food
- **More generally:** If there is a **tie** between two particular actors in **one relation**, how likely would it be to observe a **tie** between them in **another relation**?
- If two actors have a strong tie of one type, are they also likely to have a strong tie of another type?

Notes

Non-technical approach to QAP

QAP correlation...

- Tests the association between networks in two steps:
 - 1 Five measures of correlation coefficient are calculated between corresponding cells of the two matrices (called dyadic hypothesis).
 - 2 Hundreds of random permutations of rows and columns are computed while recalculating the correlation measures.
- From the second step the proportion of times that a random correlation measure is larger than or equal to the observed correlation measure is calculated.
- A lower proportion in step two (< 0.05), compared to step one, suggests a strong relationship between the matrices that is unlikely to have occurred by chance.

Notes

Intuition behind QAP

Publish together?

Observed friendship

$$\begin{pmatrix} 2 & 1 & 1 \\ 1 & 4 & 0 \\ 1 & 0 & 6 \end{pmatrix} \text{ and } \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} = \begin{array}{l} \text{Observed} \\ \text{correlation} \\ \text{measures} \\ \text{High is good!} \end{array}$$

Publish together?

Permuted friendship

$$\begin{pmatrix} 2 & 1 & 1 \\ 1 & 4 & 0 \\ 1 & 0 & 6 \end{pmatrix} \text{ and } \begin{pmatrix} ? & ? & ? \\ ? & ? & ? \\ ? & ? & ? \end{pmatrix} = \begin{array}{l} \text{Random} \\ \text{correlation} \\ \text{measures} \\ \text{High is BAD!} \end{array}$$

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Notes

Applications

- One of the most influential papers in SNA is Granovetter's (1973) "The strength of weak ties." Today we will test the first part this theory:

It is argued that the degree of overlap of two individuals' friendship networks varies directly with the strength of their tie to one another (1973, p. 1,360)

Hypothesis: The more common friends actors A and B have, the stronger the friendship tie between A and B is.

- As usual, to conduct a test in statistics we need to prepare the data.
- The data to be used is called ZACKAR and is located in UCINET.

Notes

Zachary (1977) gives to square matrices:

Observed a Karate club members for three years

- In **ZACHE** a tie is given if two individuals are friends (Binary network)
- In **ZACHC** A valued network measuring the total number of contexts in which two individuals are friend, thus measuring the strength of the friendship tie.
- These two matrices are **packed** in UCINET, meaning that the first step would be to unpack them.
- To unpack them go to **data, unpack** and select ZACKAR.



Figure 1: Unpacking procedure: outcome ZACHE and ZACHC

Notes

Matrix Algebra in SNA to obtain friends in common

Matrix multiplication creates counts from binary data

- $A * A^T$ in a **square undirected matrix** renders the number of people a given pair of actors are mutually connected to. The overlap in their personal networks

$$\begin{matrix} \text{ZACHE} & & \text{ZACHE}^T & & \text{Friends in common} \\ \begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{pmatrix} & * & \begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{pmatrix} & = & \begin{pmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 2 \end{pmatrix} \end{matrix}$$

- This is implemented in **tools,similarities** select ZACHE

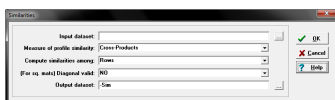
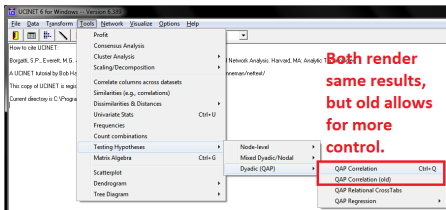


Figure 2: Similarities using matrix multiplication: outcome Friends in common

Notes

Using Friends in common and ZACHC

- We will statistically test if strength of tie (ZACH) is associated with the number of friends actors have in common



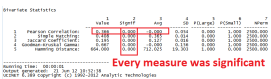
Both render same results, but old allows for more control.

Figure 3: Old and new QAP procedures

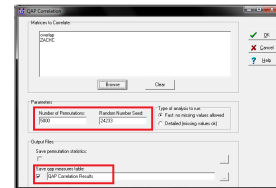
Notes



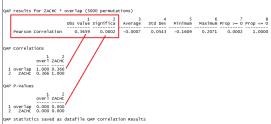
(a) Old Procedure, more flexibility



(b) More detailed measures: Pearson: numeric, Gamma: Ordinal, Simple matching and Jaccard: binary, Hamming: measure of dissimilarity



(c) New Procedure: Pearson



(d) Easier to see, but no attention to distributional form or variables?

Notes

Motivation: We may want to predict one relation knowing the other

- Which one is true?
 - Professors who publish together are friends
 - Professors are friends because they publish together
- Correlation is a symmetric association between the relations
- Regression is an asymmetric association between the relations
- **Advantage:** we can add more than one independent variable
- QAP regression uses more information to computes R-squares and Standard errors.

Notes

Regression Procedure

Several options, but most reliable is Multiple Regression Double Dekker

- The **2-step** procedure is similar as in QAP correlation.
 - 1 A standard multiple regression across corresponding cells of the dependent and independent matrices is computed.
 - 2 Randomly permutes rows and columns (together) of the matrices and recomputes the regression, storing resultant values of r-square and all coefficients.

$$\begin{array}{c} \text{Observed Outcome A} \end{array} \quad \begin{array}{c} \text{Observed Predictor B} \end{array} \quad \begin{array}{c} \text{Observed Predictor C} \end{array}$$
$$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{pmatrix} + \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{pmatrix}$$

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$$\begin{array}{c} \text{Observed Outcome A} \end{array} \quad \begin{array}{c} \text{Random Predictor B} \end{array} \quad \begin{array}{c} \text{Random Predictor C} \end{array}$$
$$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{pmatrix} = \begin{pmatrix} ? & ? & ? \\ ? & ? & ? \\ ? & ? & ? \end{pmatrix} + \begin{pmatrix} ? & ? & ? \\ ? & ? & ? \\ ? & ? & ? \end{pmatrix}$$

Notes

Data and data preparation

We will use Krack-High-Tec and the High-Tec-Attributes files

- Krackhardt's High-Tech network data (1992)
- These matrices describe three different types of ties found **among 21 managers** in a high-technology firm.
- Krack-High-Tec file contains three matrices: Advice, Friendship, and Reports To
- The High-Tec-Attributes file contains the following attributes of each of the 21 managers: Age, Tenure, Level
- Once again, we have to unpack [Data, Unpack](#)
- Select the Krack-High-Tec rendering three matrices: ADVICE, FRIENDSHIP, and REPORTS_TO

Notes

- We select **Advice** as the dependent variable
- Managers tend to ask advice only to other managers they are friends with
 - Managers tend to ask advice only to other managers they have to report to

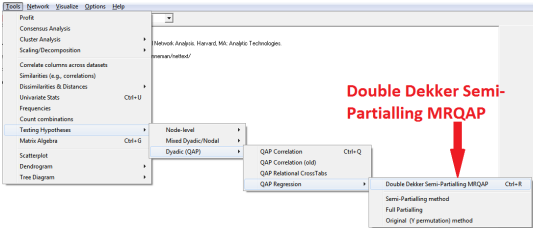
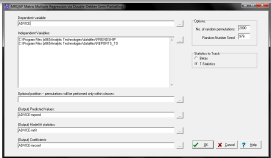


Figure 4: Follow this path or pres **ctrl + R**

Notes



(a) Options to be selected

MULTIPLE REGRESSION QAP VIA DOUBLE DEKKER SEMI-PARTIALLING

of permutations: 2000
of predictors: 2
of dependent variables: 1
of independent variables: 2
of predictors: 2
of dependent variables: 1
of independent variables: 2
of predictors: 2
of dependent variables: 1
of independent variables: 2

Model: MRQAP
Partialling: Double Dekker Semi-Partialling MRQAP
Model coefficients:
Intercept: 0.00000
FRIENDSHIP: 0.11182
REPORTS_TO: 0.11182

Model fit:
R-Square: 0.063
Adj R-Sqr: 0.000
P-value: 0.00000
Obs: 430
Pars: 3

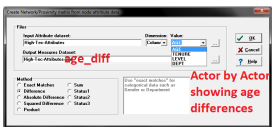
Regression coefficients:
Un-Standardized Coef: 0.11182
Standardized Coef: 0.11182
P-value: 0.00000
As Large: 0.00000
As Small: 0.00000
Std Err: 0.00000

(b) QAP regression output

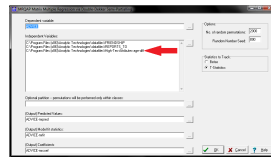
Notes



(c) Data, attribute to matrix



(d) Select age and Differences



(e) New Model Including age differences

REGRESSION COEFFICIENTS

Un-Standardized Coef: 0.11182
Standardized Coef: 0.11182
P-value: 0.00000
As Large: 0.00000
As Small: 0.00000
Std Err: 0.00000

Model fit:
R-Square: 0.063
Adj R-Sqr: 0.000
P-value: 0.00000
Obs: 430
Pars: 5

Regression coefficients:
Un-Standardized Coef: 0.11182
Standardized Coef: 0.11182
P-value: 0.00000
As Large: 0.00000
As Small: 0.00000
Std Err: 0.00000

(f) Output, what do we conclude?

Notes

Testing hypothesis. . .

Could probably be the most sub-utilized method of SNA

- The potential benefits of understanding relationships at this level of analysis are not being exploited
- New projects should be designed to test for these hypotheses, although the samples are small, the data gathering plays an important role
- New models are being developed, such as Exponential-family Random Graph Models (ERGM) implemented in the package R.

Thank you!

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